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# Search for $B_c^+$ decays to two charm mesons

LHCb Collaboration

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## Abstract

A search for decays of  $B_c^+$  mesons to two charm mesons is performed for the first time using data corresponding to an integrated luminosity of  $3.0 \text{ fb}^{-1}$ , collected by the LHCb experiment in  $pp$  collisions at centre-of-mass energies of 7 and 8 TeV. The decays considered are  $B_c^+ \rightarrow D_{(s)}^{(*)+} \bar{D}^{(*)0}$  and  $B_c^+ \rightarrow D_{(s)}^{(*)+} D^{(*)0}$ , which are normalised to high-yield  $B^+ \rightarrow D_{(s)}^+ \bar{D}^0$  decays. No evidence for a signal is found and limits are set on twelve  $B_c^+$  decay modes.

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## 1. Introduction

Flavour transitions between quarks are governed in the Standard Model (SM) of elementary particle physics by the Cabibbo–Kobayashi–Maskawa (CKM) quark-mixing matrix [1,2]. Here the transition amplitudes between up-type quarks,  $q$ , and down-type quarks,  $q'$ , are described by the complex numbers  $V_{qq'}$ , defining the  $3 \times 3$  unitary CKM matrix. Precision measurements of the magnitude and phase of the CKM matrix elements may reveal signs of new physics if observables that could be affected by new particles are found to be inconsistent with SM predictions.

One parameter of particular interest is  $\gamma \equiv \arg(-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*)$ , which can be determined experimentally with negligible theoretical uncertainties from the charge-parity ( $CP$ ) asymmetry caused by the interference between  $b \rightarrow u$  and  $b \rightarrow c$  transitions. Presently, the most precise determinations of  $\gamma$  come from measurements of the  $CP$  asymmetry in  $B^+ \rightarrow \bar{D}^0 K^+$  decays [3,4].<sup>1</sup>

<sup>1</sup> Unless specified otherwise, charge conjugation is implied throughout the paper.

Table 1

Estimates of the branching fractions of four  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$  decays in units of  $10^{-6}$ . Decays of the  $B_c^+$  meson to final states with one or two excited charm mesons have similar branching fractions and can be found in the cited references.

Channel	Prediction for the branching fraction [ $10^{-6}$ ]			
	Ref. [9]	Ref. [10]	Ref. [11]	Ref. [12]
$B_c^+ \rightarrow D_s^+ \bar{D}^0$	$2.3 \pm 0.5$	4.8	1.7	2.1
$B_c^+ \rightarrow D_s^+ D^0$	$3.0 \pm 0.5$	6.6	2.5	7.4
$B_c^+ \rightarrow D^+ \bar{D}^0$	$32 \pm 7$	53	32	33
$B_c^+ \rightarrow D^+ D^0$	$0.10 \pm 0.02$	0.32	0.11	0.32

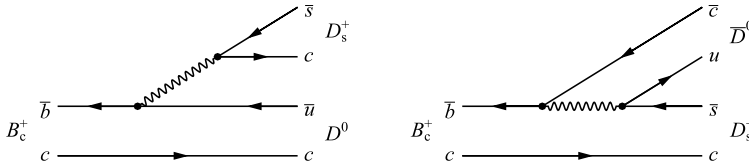


Fig. 1. Illustration of (left) a colour-favoured  $B_c^+ \rightarrow D_s^+ D^0$  decay, and (right) a colour-suppressed  $B_c^+ \rightarrow D_s^+ \bar{D}^0$  decay.

Decays of  $B_c^+$  mesons to two charm mesons,  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$ , have also been proposed to measure  $\gamma$  [5–8]. Decays with one excited charm meson in the final state,  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0$  and  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0}$ , can be used for measuring the angle  $\gamma$  in the same way as  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$  decays. For  $B_c^+$  decays with two excited charm mesons,  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0}$ , angular distributions provide an alternative method to determine  $\gamma$  [7]. Some predicted branching fractions are listed in Table 1.

In the determination of  $\gamma$ , an advantage of  $B_c^+ \rightarrow D_s^+ \bar{D}^0$  decays over  $B^+ \rightarrow \bar{D}^0 K^+$  decays is that the diagram proportional to  $V_{cb}$  is colour suppressed, while the diagram proportional to  $V_{ub}$  is not, as illustrated in Fig. 1. This results in a large value for the ratio of amplitudes,  $r_{B_c^+} \equiv |A(B_c^+ \rightarrow D^0 D_s^+)/A(B_c^+ \rightarrow \bar{D}^0 D_s^+)| \approx 1$ , and potentially in a large  $CP$  asymmetry for  $\bar{D}^0$  decays to  $CP$  eigenstates. In contrast, in  $B^+ \rightarrow \bar{D}^0 K^+$  decays, the small value of  $r_B \equiv |A(B^+ \rightarrow D^0 K^+)/A(B^+ \rightarrow \bar{D}^0 K^+)| \approx 0.1$  results in small values of the  $CP$  asymmetry. However, observing and using  $B_c^+ \rightarrow D_s^+ \bar{D}^0$  decays is challenging because of the small  $B_c^+$  production cross-section, the short  $B_c^+$  lifetime, the complex final states, and the small branching fractions.

This paper describes a search, performed for the first time, for twelve  $B_c^+ \rightarrow D_{(s)}^{(*)+} \bar{D}^{(*)0}$  decay channels, using data collected by the LHCb experiment and corresponding to an integrated luminosity of  $3.0 \text{ fb}^{-1}$ , of which  $1.0 \text{ fb}^{-1}$  was recorded at a centre-of-mass energy  $\sqrt{s} = 7 \text{ TeV}$  and  $2.0 \text{ fb}^{-1}$  at  $\sqrt{s} = 8 \text{ TeV}$ . Charm mesons are reconstructed in the  $D^0 \rightarrow K^- \pi^+$ ,  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$ ,  $D^+ \rightarrow K^- \pi^+ \pi^+$ , and  $D_s^+ \rightarrow K^+ K^- \pi^+$  decay modes. For  $B_c^+$  decays that involve one or more excited charm mesons, no attempt is made to reconstruct the low-momentum particles from the decay of excited charm mesons: the distribution of the invariant mass of the partially reconstructed final-state peaks at masses just below the  $B_c^+$  mass.

The branching fractions,  $\mathcal{B}$ , of  $B_c^+$  decays to fully reconstructed states are measured relative to high-yield  $B^+ \rightarrow D_{(s)}^+ \bar{D}^0$  normalisation modes,

$$\frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0)}{\mathcal{B}(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)} = \frac{N(B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0)}{N(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)} \frac{\varepsilon(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)}{\varepsilon(B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0)}, \quad (1)$$

where  $f_c/f_u$  is the ratio of  $B_c^+$  to  $B^+$  production cross-sections,  $N$  stands for the signal yields, and  $\varepsilon$  for the total efficiencies. For  $B_c^+$  decays with one excited charm meson, the invariant-mass distributions of  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0$  and  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0}$  decays are very similar, and the sum of their branching fractions is measured, weighted by the branching fraction of the excited charged charm meson to a charged charm meson and a low-momentum neutral particle,  $\mathcal{B}(D_{(s)}^{*+} \rightarrow D_{(s)}^+ \pi^0, \gamma)$ ,

$$\begin{aligned} \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0) \mathcal{B}(D_{(s)}^{*+} \rightarrow D_{(s)}^+ \pi^0, \gamma) + \mathcal{B}(B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0})}{\mathcal{B}(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)} = \\ \frac{N(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0) + N(B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0})}{N(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)} \frac{\varepsilon(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)}{\varepsilon(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0, D_{(s)}^+ \bar{D}^{*0})}, \end{aligned} \quad (2)$$

where  $\varepsilon(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0, D_{(s)}^+ \bar{D}^{*0})$  is the average efficiency of  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0$  and  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0}$  decays. Branching fractions of  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0$  are corrected for  $\mathcal{B}(D_{(s)}^{*+} \rightarrow D_{(s)}^+ \pi^0, \gamma)$ ,

$$\begin{aligned} \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0})}{\mathcal{B}(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)} = \\ \frac{1}{\mathcal{B}(D_{(s)}^{*+} \rightarrow D_{(s)}^+ \pi^0, \gamma)} \frac{N(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0})}{N(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)} \frac{\varepsilon(B^+ \rightarrow D_{(s)}^+ \bar{D}^0)}{\varepsilon(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0})}. \end{aligned} \quad (3)$$

LHCb measurements of  $(f_c \mathcal{B}(B_c^+ \rightarrow J/\psi \pi^+))/(f_u \mathcal{B}(B^+ \rightarrow J/\psi K^+))$  show no significant difference of  $f_c/f_u$  between  $\sqrt{s} = 7 \text{ TeV}$  [13] and  $\sqrt{s} = 8 \text{ TeV}$  [14] in the LHCb acceptance. Predictions for  $\mathcal{B}(B_c^+ \rightarrow J/\psi \pi^+)$  range from  $6.0 \times 10^{-4}$  to  $2.9 \times 10^{-3}$  [15–17], implying a value of  $f_c/f_u$  in the range 0.24%–1.2%. Since  $\mathcal{B}(B_c^+ \rightarrow J/\psi \pi^+)$  is presently not measured, the results in this paper are expressed as the product of  $f_c/f_u$  and the ratio of  $B_c^+$  to  $B^+$  branching fractions.

## 2. Detector and simulation

The LHCb detector [18,19] is a single-arm forward spectrometer covering the pseudorapidity range  $2 < \eta < 5$ , designed for the study of particles containing  $b$  or  $c$  quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the  $pp$  interaction region [20], a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes [21] placed downstream of the magnet. The polarity of the dipole magnet is reversed periodically throughout data-taking.

The tracking system provides a measurement of the momentum of charged particles with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV/ $c$ . The minimum distance of a track to a primary  $pp$  interaction vertex (PV), the impact parameter (IP), is measured with a resolution of  $(15 + 29/p_T) \mu\text{m}$ , where  $p_T$  is the momentum transverse to

the beamline expressed in GeV/c. Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors [22]. Photons, electrons and hadrons are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers [23].

The online event selection is performed by a trigger [24], which consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction. At the hardware trigger stage, events are required to have a muon with high  $p_T$  or a hadron, photon or electron with high transverse energy in the calorimeters. For hadrons, the transverse energy threshold is about 3.5 GeV. The software trigger requires a two-, three- or four-track secondary vertex with a large sum of the transverse momentum of the tracks and a significant displacement from any PV. At least one track should have  $p_T > 1.7$  GeV/c and  $\chi_{\text{IP}}^2$  with respect to any PV greater than 16, where  $\chi_{\text{IP}}^2$  is defined as the difference in the vertex-fit  $\chi^2$  of a given PV reconstructed with and without the considered particle. A multivariate algorithm [25] is used for the identification of secondary vertices consistent with the decay of a  $b$  hadron.

Simulated events are used for the training of the multivariate selection of the  $B_c^+$  signals, for establishing the shape of the invariant-mass distributions of the signals, and for determining the relative efficiency between the  $B_c^+$  signal decays and the  $B^+$  normalisation modes. In the simulation,  $pp$  collisions with  $B^+ \rightarrow D_{(s)}^+ \bar{D}^0$  decays are generated using PYTHIA [26] with a specific LHCb configuration [27]. For  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$  decays, the BCVEGPY [28] generator is used. The simulated  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$  sample is also used for training and efficiency calculations of the  $B_c^+ \rightarrow D_{(s)}^+ D^0$  decay mode. Decays of hadronic particles are described by EVTGEN [29], with final-state radiation generated using PHOTOS [30]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [31] as described in Ref. [32]. Known discrepancies in the simulation are corrected using data-driven methods.

### 3. Candidate selection

Initially, loose requirements are made to select candidates having both a  $D_{(s)}^+$  and a  $D^0$  or  $\bar{D}^0$  meson. The charm-meson candidates are constructed by combining two, three or four tracks that are incompatible with originating from any reconstructed PV. In addition, the tracks must form a high-quality vertex and the scalar sum of their transverse momenta must exceed 1.8 GeV/c. The pion and kaon candidates are also required to satisfy loose particle identification (PID) criteria to reduce the contribution to the selected sample from misidentified particles. Charm-meson candidates must have an invariant mass within  $\pm 25$  MeV/ $c^2$  of their known value [33]. Using the same method as in Ref. [34], three-track combinations that are compatible with both  $D^+ \rightarrow K^- \pi^+ \pi^+$  and  $D_s^+ \rightarrow K^+ K^- \pi^+$  decays are categorised as a  $D_s^+$  candidate if the  $K^+ K^-$  combination is compatible with the  $\phi \rightarrow K^+ K^-$  decay or if the  $K^+$  candidate satisfies strict PID criteria, and as a  $D^+$  candidate otherwise. The two charm mesons are combined into a  $B_{(c)}^+$  candidate, which is retained if its invariant mass is in the range 4.8–7.0 GeV/ $c^2$ . The  $D_{(s)}^+ \bar{D}^0$  pair must form a good-quality vertex with transverse momentum exceeding 4.0 GeV/c. The resulting trajectory of the  $B_{(c)}^+$  candidate must be consistent with originating from the associated PV, where the associated PV is the PV with which the  $B_{(c)}^+$  candidate has the smallest  $\chi_{\text{IP}}^2$ . The reconstructed decay time

divided by its uncertainty,  $t/\sigma_t$ , of  $D^0$  and  $D_s^+$  mesons with respect to the  $B_{(c)}^+$  vertex is required to exceed  $-3$ , while that of the longer-lived  $D^+$  meson is required to exceed  $+3$ . The tighter decay-time significance criterion on the  $D^+$  eliminates background from  $B^+ \rightarrow \bar{D}^0 \pi^+ \pi^- \pi^+$  decays where the negatively charged pion is misidentified as a kaon.

The invariant-mass resolution of  $B_{(c)}^+$  decays is significantly improved by applying a kinematic fit [35] where the masses of the  $D^0$  and the  $D_{(s)}^+$  candidates are fixed to their known values [33], all particles from the  $D_{(s)}^+$ ,  $D^0$ , or  $B_{(c)}^+$  decay are constrained to originate from their decay vertex and the  $B_{(c)}^+$  is constrained to originate from a PV.

To reduce the combinatorial background, while keeping the efficiency for signal as high as possible, a multivariate selection based on a boosted decision tree (BDT) [36,37] is employed. The following variables are used as input for the BDT: the transverse momentum and the ratio of the likelihood between the kaon and pion PID hypotheses of all final-state particles; the fit quality of the  $B_{(c)}^+$  and both charm-meson vertices; the value of  $\chi_{\text{IP}}^2$  of the  $B_{(c)}^+$  candidate; the values of  $t/\sigma_t$  of the  $B_{(c)}^+$  and both charm-meson candidates; the invariant masses of the reconstructed charm-meson candidates; and the invariant masses of the pairs of opposite-charge tracks from the  $D_{(s)}^+$  candidate.

Four distinct classifiers are constructed: the BDT training is performed separately for the  $D_s^+ \bar{D}^0$  and  $D^+ \bar{D}^0$  final states and for the  $D^0 \rightarrow K^- \pi^+$  and  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  decay channels. For a given  $D^0$  final state, the same classifier is used for both  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$  and  $B_c^+ \rightarrow D_{(s)}^+ D^0$  decays. For signal, the BDT is trained using simulated  $B_c^+$  events, while for background data in the range  $5350 < m(D_{(s)}^+ \bar{D}^0) < 6200 \text{ MeV}/c^2$  are used. Studies indicate that the combinatorial background is dominated by non-charm and single-charm candidates, while combinations of two real charm mesons contribute less than 5%. To increase the size of the background sample for the BDT training, the charm mass windows are increased from  $\pm 25 \text{ MeV}/c^2$  to  $\pm 75 \text{ MeV}/c^2$ .

The BDT combines all input variables into a single discriminant. The optimal value of the cut on this discriminant is determined using a procedure based on Ref. [38], maximising  $\varepsilon/(\sqrt{N_B} + 5/2)$ , where  $N_B$  is the expected background in a  $\pm 20 \text{ MeV}/c^2$  window around the  $B_c^+$  mass, and the number 5 is the target significance. Simulated events are used to estimate the signal efficiency  $\varepsilon$ .

#### 4. Data fit

After the selection, a model of the invariant-mass distribution of  $B_{(c)}^+ \rightarrow D_{(s)}^+ \bar{D}^0$  candidates is fitted to the data. The model is composed of six components: the signals for fully reconstructed  $B^+$  and  $B_c^+$  decays; the signal for  $B_c^+$  decays with one excited charm meson in the final state; the signal for  $B_c^+$  decays with two excited charm mesons in the final state; the background from  $B^+ \rightarrow \bar{D}^0 K^+ K^- \pi^+$  decays; and the combinatorial background.

Fully reconstructed  $B^+$  and  $B_c^+$  signals are described by the sum of two Crystal Ball (CB) [39] functions, with power-law tails proportional to  $[m(D_{(s)}^+ \bar{D}^0) - m(B_{(c)}^+)]^{-2}$  in opposite directions. The peak values of both CB components are constrained to be equal and the other shape parameters of the CB functions are obtained from a fit to the simulated events. The peak position of the  $B^+$  signal is a free parameter in the fit to data, while the peak position of the  $B_c^+$  signal is fixed to the world-average measurement [33]. The large  $B^+ \rightarrow D_s^+ \bar{D}^0$  signal from data is well described by this model.

Table 2

Ratio  $\varepsilon_{B_c^+}/\varepsilon_{B^+}$  of total efficiencies of  $B_c^+$  decays relative to the corresponding fully reconstructed  $B^+$  decays. The quoted uncertainties are statistical only.

Decay channel	Reconstructed state			
	$D_s^+ \bar{D}^0$ with $D^0 \rightarrow$		$D^+ \bar{D}^0$ with $D^0 \rightarrow$	
	$K^- \pi^+$	$K^- \pi^+ \pi^- \pi^+$	$K^- \pi^+$	$K^- \pi^+ \pi^- \pi^+$
$B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$	$0.420 \pm 0.005$	$0.373 \pm 0.009$	$0.441 \pm 0.007$	$0.398 \pm 0.010$
$B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0, D_{(s)}^+ \bar{D}^{*0}$	$0.372 \pm 0.006$	$0.317 \pm 0.010$	$0.381 \pm 0.008$	$0.337 \pm 0.011$
$B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0}$	$0.339 \pm 0.006$	$0.278 \pm 0.009$	$0.342 \pm 0.007$	$0.297 \pm 0.010$

Models for decays where one or two low-momentum particles from excited charm-meson decays are missing are implemented as templates, obtained from invariant-mass distributions of simulated data. For decays with one missing low-momentum particle, both  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0$  and  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0}$  decays contribute and the template is based on the sum of the two decay modes, weighted by the appropriate branching fractions of the excited charm mesons. For  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0}$  decays, it is assumed that both excited charm mesons are produced unpolarised.

The Cabibbo-favoured  $B^+ \rightarrow \bar{D}^0 K^+ K^- \pi^+$  decay is a background to the  $B^+ \rightarrow D_s^+ \bar{D}^0$  channel, though its yield is strongly reduced by the charm-meson mass requirement. This background is modelled by a single Gaussian function, with the width determined from a sample of simulated decays and the normalisation determined from the sidebands of the  $D_s^+$  mass peak. The yield of this background is about 40 times smaller than that of the signal, and the shape of the invariant-mass distribution is twice as wide. The combinatorial background is described by the sum of an exponential function and a constant.

An unbinned extended maximum likelihood fit is used to simultaneously describe the invariant-mass distributions of candidates with  $D^0 \rightarrow K^- \pi^+$  and  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  decays, resulting in four independent fits to eight invariant mass distributions. In these fits the background parameters and  $B^+$  yields are free to vary independently, but the ratio of the  $B_c^+$  yields for the two  $D^0$  decay modes is constrained to the corresponding ratio of  $B^+$  yields, corrected for the relative efficiencies. The total  $B_c^+$  yield,  $N_{B_c^+}^{\text{tot}}$ , is a free parameter in these fits, leading to a  $B_c^+$  yield in each data sample given by the expressions

$$N_{B_c^+}^{K\pi} = \frac{N_{B^+}^{K\pi} \varepsilon_{B_c^+}^{K\pi} / \varepsilon_{B^+}^{K\pi}}{N_{B^+}^{K\pi} \varepsilon_{B_c^+}^{K\pi} / \varepsilon_{B^+}^{K\pi} + N_{B^+}^{K\pi\pi\pi} \varepsilon_{B_c^+}^{K\pi\pi\pi} / \varepsilon_{B^+}^{K\pi\pi\pi}} N_{B_c^+}^{\text{tot}}, \quad (4)$$

$$N_{B_c^+}^{K\pi\pi\pi} = \frac{N_{B^+}^{K\pi\pi\pi} \varepsilon_{B_c^+}^{K\pi\pi\pi} / \varepsilon_{B^+}^{K\pi\pi\pi}}{N_{B^+}^{K\pi} \varepsilon_{B_c^+}^{K\pi} / \varepsilon_{B^+}^{K\pi} + N_{B^+}^{K\pi\pi\pi} \varepsilon_{B_c^+}^{K\pi\pi\pi} / \varepsilon_{B^+}^{K\pi\pi\pi}} N_{B_c^+}^{\text{tot}}. \quad (5)$$

The relative efficiencies that appear in these expressions, calculated for simulated events generated in the rapidity range  $2.0 < y(B_{(c)}^+) < 4.5$  and with  $p_T(B_{(c)}^+) > 4 \text{ GeV}/c$ , are summarised in Table 2.

The results of the fits are shown in Fig. 2, and the corresponding signal yields are listed in Table 3. The small peaks at the  $B^+$  mass in the  $D_{(s)}^+ \bar{D}^0$  final state are due to  $B^+ \rightarrow D_{(s)}^+ \bar{D}^0$  decays either followed by the doubly Cabibbo-suppressed  $D^0 \rightarrow K^+ \pi^-$  decay or when both the

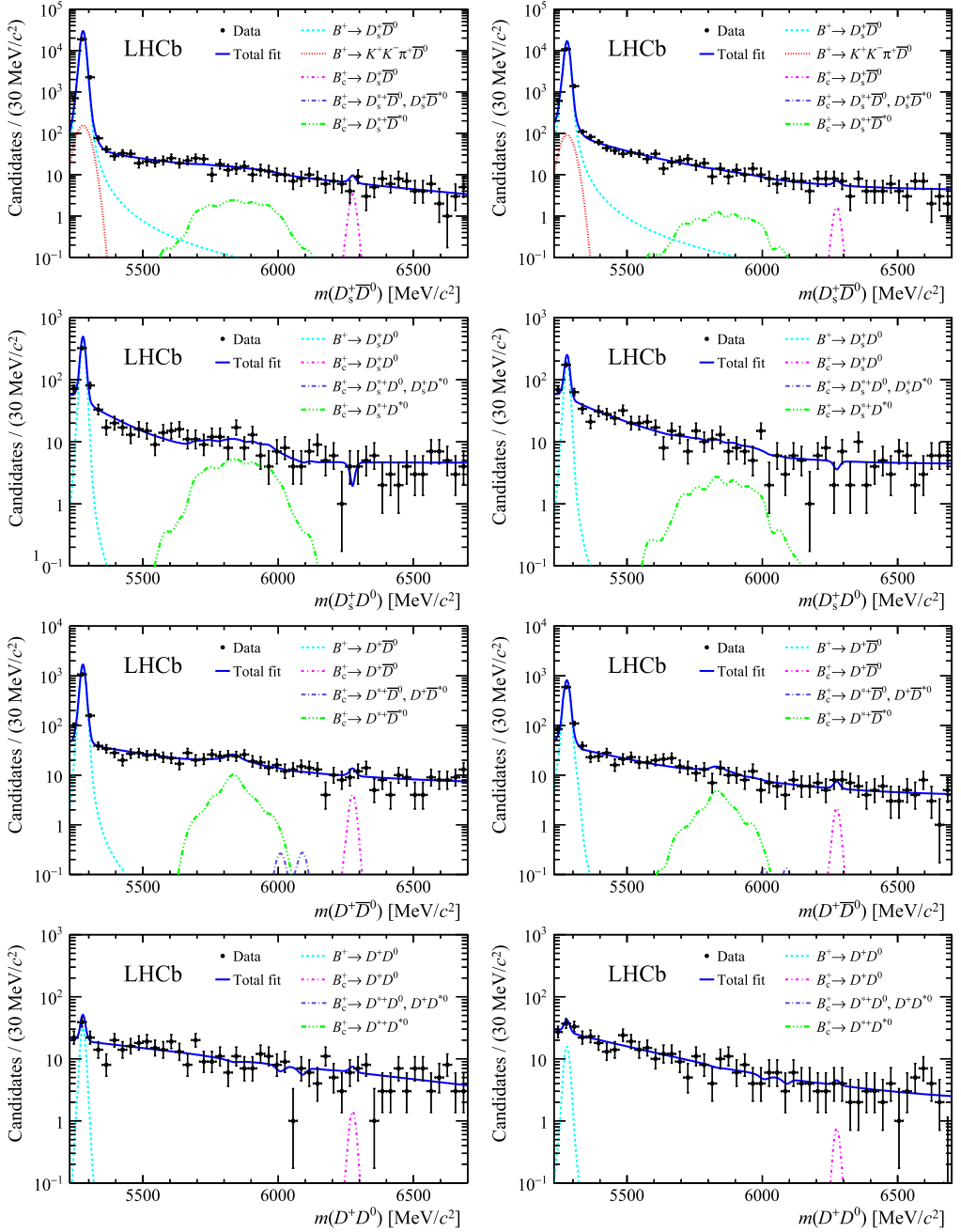


Fig. 2. Fits to the (top row)  $D_s^+ \bar{D}^0$ , (second row)  $D_s^+ D^0$ , (third row)  $D^+ \bar{D}^0$  and (bottom row)  $D^+ D^0$  final states. For the left plots, the  $D^0$  meson is reconstructed in the  $K^- \pi^+$  final state, while the right column corresponds to the  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  mode.



Table 3

Signal yields from the fits of  $B \rightarrow D_{(s)}^+ (\overline{D})^0$  decays. Samples with  $D^0 \rightarrow K^- \pi^+$  and  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  are fitted simultaneously. The uncertainties are statistical only.

Decay channel	Reconstructed state			
	$D_s^+ \overline{D}^0$	$D_s^+ D^0$	$D^+ \overline{D}^0$	$D^+ D^0$
$B^+ \rightarrow D_{(s)}^+ \overline{D}^0$	$33\,734 \pm 187$	$476 \pm 27$	$1866 \pm 46$	$37 \pm 11$
$B_c^+ \rightarrow D_{(s)}^+ (\overline{D})^0$	$5 \pm 5$	$-4 \pm 3$	$6 \pm 6$	$2 \pm 4$
$B_c^+ \rightarrow D_{(s)}^{*+} (\overline{D})^0, D_{(s)}^+ (\overline{D})^{*0}$	$-1 \pm 14$	$-4 \pm 10$	$1 \pm 13$	$-10 \pm 9$
$B_c^+ \rightarrow D_{(s)}^{*+} (\overline{D})^{*0}$	$34 \pm 28$	$73 \pm 19$	$68 \pm 23$	$-8 \pm 14$

Table 4

Systematic uncertainties on the  $B_c^+$  yields, for the combined fit to both the  $D^0 \rightarrow K^- \pi^+$  and the  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  decay channels. The total systematic uncertainty is calculated as the quadratic sum of the individual components.

Source	Reconstructed state			
	$D_s^+ \overline{D}^0$	$D_s^+ D^0$	$D^+ \overline{D}^0$	$D^+ D^0$
$B_c^+ \rightarrow D_{(s)}^+ (\overline{D})^0$				
Signal shape	0.25	0.28	0.31	0.13
Signal model	0.40	0.34	0.61	0.44
$B_c^+$ mass	0.64	0.62	0.79	0.51
Background model	1.12	1.75	1.88	0.56
Fit bias	0.70	1.28	0.27	0.19
Total	1.54	2.30	2.17	0.91
$B_c^+ \rightarrow D_{(s)}^{*+} (\overline{D})^0, D_{(s)}^+ (\overline{D})^{*0}$				
Signal composition	7.6	5.5	7.1	5.7
Background model	11.9	17.5	16.4	4.5
Fit bias	5.5	9.4	3.9	1.3
Total	15.2	20.6	18.3	7.4
$B_c^+ \rightarrow D_{(s)}^{*+} (\overline{D})^{*0}$				
Polarisation	23	14	9	5
Background model	43	98	37	9
Fit bias	10	7	8	1
Total	49	99	39	10

kaon and pion are misidentified. No significant  $B_c^+$  signals are observed; after taking into account systematic uncertainties, discussed in Sec. 5, none of the signals exceeds a significance of two standard deviations, which is measured as the difference in likelihood when fitting the data with or without signal component in the fit [40].

## 5. Systematic uncertainties

The systematic uncertainties on the  $B_c^+$  yields are listed in Table 4 and described below. The signal shape parameters for the fully reconstructed modes are varied according to Gaussian distributions that take into account the covariance matrix of the fit to the simulated events, and

Table 5

Systematic uncertainties, in %, on the normalisation of the  $B_c^+$  branching fraction determination. The total systematic uncertainty is calculated as the quadratic sum of the individual components.

Channel	Source	Reconstructed state			
		$D_s^+ \bar{D}^0$ , with $D^0 \rightarrow$		$D^+ \bar{D}^0$ , with $D^0 \rightarrow$	
		$K^- \pi^+$	$K^- \pi^+ \pi^- \pi^+$	$K^- \pi^+$	$K^- \pi^+ \pi^- \pi^+$
Common	$B^+$ stat.	0.7	0.9	3.1	4.3
	$B^+$ signal shape	0.0	0.0	0.0	0.3
	$B^+$ signal model	0.1	0.2	0.1	0.3
	Background model	0.0	0.6	1.6	1.3
	$B^+ \rightarrow \bar{D}^0 K^+ K^- \pi^+$	1.4	1.4	–	–
	$B_c^+$ lifetime	1.5	1.5	1.5	1.5
	PID	2.4	0.9	1.2	3.2
	$D^0$ model	–	1.1	–	0.7
$B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$	Simulation stat.	1.2	2.4	1.6	2.5
	Total	3.5	3.6	4.3	6.3
$B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0, D_{(s)}^+ \bar{D}^{*0}$	Simulation stat.	1.7	3.3	2.0	3.3
	Signal composition	1.0	0.8	0.7	2.6
	Total	3.8	4.3	4.5	7.1
$B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0}$	Simulation stat.	1.7	3.4	2.0	3.3
	Polarisation	1.5	0.4	1.4	1.3
	$\mathcal{B}(D^{*+} \rightarrow D^+ \pi^0, \gamma)$	–	–	1.5	1.5
	Total	3.9	4.4	4.9	6.9

evaluating the change in yield and its uncertainty for 1000 variations. An additional uncertainty is attributed to the signal model by changing its description from a sum of two CB functions to a sum of two Gaussian functions. The assumed peak position of the  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^0$  signal may differ from the true value. This is taken into account by varying the  $B_c^+$  peak position by its uncertainty, taken as the squared sum of uncertainty on the world-average  $B_c^+$  mass ( $0.8 \text{ MeV}/c^2$ ) and the contribution from the LHCb momentum-scale uncertainty ( $0.8 \text{ MeV}/c^2$ ) [41]. The signal shape of the decays with one missing low-momentum particle is based on the assumption  $\mathcal{B}(B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0) = \mathcal{B}(B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0})$ . Since the  $B_c^+$  branching fractions are unknown, the signal composition is varied using  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^0$  or  $B_c^+ \rightarrow D_{(s)}^+ \bar{D}^{*0}$  only and the largest difference is taken as the systematic uncertainty. As the polarisation of excited charm mesons in  $B_c^+ \rightarrow D_{(s)}^{*+} \bar{D}^{*0}$  decays is unknown, the signal shapes are varied between fully longitudinal and fully transverse polarisations, and the largest yield difference with the unpolarised decay model is taken as the uncertainty. To evaluate the uncertainty in the choice of the shape of the combinatorial background, an alternative fit is applied using an exponential function to model the background. To evaluate eventual biases of the  $B_c^+$  yields in the fit, pseudoexperiments are generated where the candidates in the signal window are replaced by the expected distribution using only background. The yields are corrected for this bias and the attributed uncertainty is the squared sum of the bias and its statistical uncertainty.

Systematic uncertainties that affect the normalisation are listed in Table 5 and are described below. The limited size of the simulated signal samples affects the normalisation as well as the

statistical uncertainties of the  $B^+$  yields. The systematic uncertainties of the  $B^+$  yields are evaluated by varying the signal shape according to the covariance matrix of the fit to simulated data and by changing the signal model to the sum of two Gaussian functions. The  $B^+$  yield is also affected by uncertainties on the background, which are evaluated by changing the background shape to an exponential function and by varying the single-charm background by 100% of its yield. The impact on the efficiency ratio of the uncertainty on the  $B_c^+$  lifetime is evaluated by changing its lifetime by one standard deviation. Imperfections in the rescaling of the PID variables [22] are quantified by considering the efficiency ratio with and without PID corrections and assigning the difference as a systematic uncertainty. The  $D^0 \rightarrow K^-\pi^+\pi^-\pi^+$  decay has a complicated substructure, but was simulated according to a phase-space model. The systematic uncertainty is taken as the quadratic sum of the differences in efficiency ratio when the simulated events are weighted to reproduce the  $\pi^+\pi^-$ ,  $K^-\pi^+$ ,  $K^-\pi^+\pi^-$  and  $\pi^+\pi^-\pi^+$  invariant-mass distributions observed in data. The difference in efficiency when applying the model variations for  $B_c^+$  decays with one or two excited charm mesons in the final state is taken into account as a systematic uncertainty. The determinations of the  $B_c^+ \rightarrow D^{*+}\bar{D}^{*0}$  branching fraction ratios are corrected for  $\mathcal{B}(D^{*+} \rightarrow D^+\pi^0, \gamma) = (32.3 \pm 0.5)\%$  [33], as is indicated in Eq. (3), and the corresponding uncertainty is assigned as a systematic uncertainty.

## 6. Results and conclusion

To determine the branching fraction ratios, fits to data are performed where the free parameters are not the individual yields, but correspond to the left-hand-side terms of Eqs. (1)–(3). In these fits, the systematic uncertainties are taken into account as Gaussian constraints.

The measured branching fraction ratios for the fully reconstructed  $B_c^+$  decays are listed below. Quoted in brackets are the corresponding upper limits calculated at 90% (95%) confidence level with the asymptotic CL<sub>s</sub> method [42],

$$\begin{aligned} \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_s^+\bar{D}^0)}{\mathcal{B}(B^+ \rightarrow D_s^+\bar{D}^0)} &= (3.0 \pm 3.7) \times 10^{-4} [< 0.9 (1.1) \times 10^{-3}], \\ \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_s^+D^0)}{\mathcal{B}(B^+ \rightarrow D_s^+\bar{D}^0)} &= (-3.8 \pm 2.6) \times 10^{-4} [< 3.7 (4.7) \times 10^{-4}], \\ \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D^+\bar{D}^0)}{\mathcal{B}(B^+ \rightarrow D^+\bar{D}^0)} &= (8.0 \pm 7.5) \times 10^{-3} [< 1.9 (2.2) \times 10^{-2}], \\ \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D^+D^0)}{\mathcal{B}(B^+ \rightarrow D^+\bar{D}^0)} &= (2.9 \pm 5.3) \times 10^{-3} [< 1.2 (1.4) \times 10^{-2}]. \end{aligned}$$

For  $B_c^+$  decays with one excited charm meson, the results are

$$\begin{aligned} \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_s^{*+}\bar{D}^0) + \mathcal{B}(B_c^+ \rightarrow D_s^+\bar{D}^{*0})}{\mathcal{B}(B^+ \rightarrow D_s^+\bar{D}^0)} &= \\ &= (-0.1 \pm 1.5) \times 10^{-3} [< 2.8 (3.4) \times 10^{-3}], \\ \frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_s^{*+}D^0) + \mathcal{B}(B_c^+ \rightarrow D_s^+D^{*0})}{\mathcal{B}(B^+ \rightarrow D_s^+\bar{D}^0)} &= \\ &= (-0.3 \pm 1.9) \times 10^{-3} [< 3.0 (3.6) \times 10^{-3}], \end{aligned}$$

$$\frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow (D^{*+} \rightarrow D^+ \pi^0, \gamma) \bar{D}^0) + \mathcal{B}(B_c^+ \rightarrow D^+ \bar{D}^{*0})}{\mathcal{B}(B^+ \rightarrow D^+ \bar{D}^0)} =$$

$$(0.2 \pm 3.2) \times 10^{-2} [< 5.5 (6.6) \times 10^{-2}],$$

$$\frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow (D^{*+} \rightarrow D^+ \pi^0, \gamma) D^0) + \mathcal{B}(B_c^+ \rightarrow D^+ D^{*0})}{\mathcal{B}(B^+ \rightarrow D^+ \bar{D}^0)} =$$

$$(-1.5 \pm 1.7) \times 10^{-2} [< 2.2 (2.8) \times 10^{-2}].$$

For  $B_c^+$  decays with two excited charm mesons, the measurements give

$$\frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_s^{*+} \bar{D}^{*0})}{\mathcal{B}(B^+ \rightarrow D_s^+ \bar{D}^0)} = (3.2 \pm 4.3) \times 10^{-3} [< 1.1 (1.3) \times 10^{-2}],$$

$$\frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D_s^{*+} D^{*0})}{\mathcal{B}(B^+ \rightarrow D_s^+ \bar{D}^0)} = (7.0 \pm 9.2) \times 10^{-3} [< 2.0 (2.4) \times 10^{-2}],$$

$$\frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D^{*+} \bar{D}^{*0})}{\mathcal{B}(B^+ \rightarrow D^+ \bar{D}^0)} = (3.4 \pm 2.3) \times 10^{-1} [< 6.5 (7.3) \times 10^{-1}],$$

$$\frac{f_c}{f_u} \frac{\mathcal{B}(B_c^+ \rightarrow D^{*+} D^{*0})}{\mathcal{B}(B^+ \rightarrow D^+ \bar{D}^0)} = (-4.1 \pm 9.1) \times 10^{-2} [< 1.3 (1.6) \times 10^{-1}].$$

The presented limits are consistent with the theoretical expectations: assuming a value of  $f_c/f_u = 1.2\%$ , the branching fraction ratio limits give  $\mathcal{B}(B_c^+ \rightarrow D^+ \bar{D}^0) < 6.0 (7.0) \times 10^{-4}$  at 90% (95%) confidence level, well above the values shown in Table 1.

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 V. Cogoni<sup>16,f</sup>, L. Cojocariu<sup>30</sup>, P. Collins<sup>40</sup>, T. Colombo<sup>40</sup>,  
 A. Comerma-Montells<sup>12</sup>, A. Contu<sup>16</sup>, G. Coombs<sup>40</sup>, S. Coquereau<sup>38</sup>,  
 G. Corti<sup>40</sup>, M. Corvo<sup>17,g</sup>, C.M. Costa Sobral<sup>50</sup>, B. Couturier<sup>40</sup>,  
 G.A. Cowan<sup>52</sup>, D.C. Craik<sup>58</sup>, A. Crocombe<sup>50</sup>, M. Cruz Torres<sup>1</sup>,  
 R. Currie<sup>52</sup>, C. D'Ambrosio<sup>40</sup>, F. Da Cunha Marinho<sup>2</sup>, C.L. Da Silva<sup>72</sup>,  
 E. Dall'Occo<sup>43</sup>, J. Dalseno<sup>48</sup>, A. Davis<sup>3</sup>, O. De Aguiar Francisco<sup>40</sup>,  
 K. De Bruyn<sup>40</sup>, S. De Capua<sup>56</sup>, M. De Cian<sup>12</sup>, J.M. De Miranda<sup>1</sup>,  
 L. De Paula<sup>2</sup>, M. De Serio<sup>14,d</sup>, P. De Simone<sup>19</sup>, C.T. Dean<sup>53</sup>,  
 D. Decamp<sup>4</sup>, L. Del Buono<sup>8</sup>, H.-P. Dembinski<sup>11</sup>, M. Demmer<sup>10</sup>,  
 A. Dendek<sup>28</sup>, D. Derkach<sup>35</sup>, O. Deschamps<sup>5</sup>, F. Dettori<sup>54</sup>, B. Dey<sup>65</sup>,  
 A. Di Canto<sup>40</sup>, P. Di Nezza<sup>19</sup>, H. Dijkstra<sup>40</sup>, F. Dordei<sup>40</sup>, M. Dorigo<sup>40</sup>,  
 A. Dosil Suárez<sup>39</sup>, L. Douglas<sup>53</sup>, A. Dovbnya<sup>45</sup>, K. Dreimanis<sup>54</sup>,  
 L. Dufour<sup>43</sup>, G. Dujany<sup>8</sup>, P. Durante<sup>40</sup>, J.M. Durham<sup>72</sup>, D. Dutta<sup>56</sup>,  
 R. Dzhelyadin<sup>37</sup>, M. Dziewiecki<sup>12</sup>, A. Dziurda<sup>40</sup>, A. Dzyuba<sup>31</sup>,  
 S. Easo<sup>51</sup>, M. Ebert<sup>52</sup>, U. Egede<sup>55</sup>, V. Egorychev<sup>32</sup>, S. Eidelman<sup>36,w</sup>,  
 S. Eisenhardt<sup>52</sup>, U. Eitschberger<sup>10</sup>, R. Ekelhof<sup>10</sup>, L. Eklund<sup>53</sup>, S. Ely<sup>61</sup>,  
 S. Esen<sup>12</sup>, H.M. Evans<sup>49</sup>, T. Evans<sup>57</sup>, A. Falabella<sup>15</sup>, N. Farley<sup>47</sup>,  
 S. Farry<sup>54</sup>, D. Fazzini<sup>21,i</sup>, L. Federici<sup>25</sup>, D. Ferguson<sup>52</sup>, G. Fernandez<sup>38</sup>,  
 P. Fernandez Declara<sup>40</sup>, A. Fernandez Prieto<sup>39</sup>, F. Ferrari<sup>15</sup>,  
 L. Ferreira Lopes<sup>41</sup>, F. Ferreira Rodrigues<sup>2</sup>, M. Ferro-Luzzi<sup>40</sup>,  
 S. Filippov<sup>34</sup>, R.A. Fini<sup>14</sup>, M. Fiorini<sup>17,g</sup>, M. Firlej<sup>28</sup>, C. Fitzpatrick<sup>41</sup>,  
 T. Fiutowski<sup>28</sup>, F. Fleuret<sup>7,b</sup>, M. Fontana<sup>16,40</sup>, F. Fontanelli<sup>20,h</sup>,  
 R. Forty<sup>40</sup>, V. Franco Lima<sup>54</sup>, M. Frank<sup>40</sup>, C. Frei<sup>40</sup>, J. Fu<sup>22,q</sup>,  
 W. Funk<sup>40</sup>, E. Furfaro<sup>25,j</sup>, C. Färber<sup>40</sup>, E. Gabriel<sup>52</sup>, A. Gallas Torreira<sup>39</sup>,  
 D. Galli<sup>15,e</sup>, S. Gallorini<sup>23</sup>, S. Gambetta<sup>52</sup>, M. Gandelman<sup>2</sup>, P. Gandini<sup>22</sup>,  
 Y. Gao<sup>3</sup>, L.M. Garcia Martin<sup>70</sup>, J. García Pardiñas<sup>39</sup>, J. Garra Tico<sup>49</sup>,  
 L. Garrido<sup>38</sup>, D. Gascon<sup>38</sup>, C. Gaspar<sup>40</sup>, L. Gavardi<sup>10</sup>, G. Gazzoni<sup>5</sup>,



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 S. Gianì<sup>41</sup>, V. Gibson<sup>49</sup>, O.G. Girard<sup>41</sup>, L. Giubega<sup>30</sup>, K. Gizdov<sup>52</sup>,  
 V.V. Gligorov<sup>8</sup>, D. Golubkov<sup>32</sup>, A. Golutvin<sup>55</sup>, A. Gomes<sup>1,a</sup>,  
 I.V. Gorelov<sup>33</sup>, C. Gotti<sup>21,i</sup>, E. Govorkova<sup>43</sup>, J.P. Grabowski<sup>12</sup>,  
 R. Graciani Diaz<sup>38</sup>, L.A. Granado Cardoso<sup>40</sup>, E. Graugés<sup>38</sup>,  
 E. Graverini<sup>42</sup>, G. Graziani<sup>18</sup>, A. Greco<sup>30</sup>, R. Greim<sup>9</sup>, P. Griffith<sup>16</sup>,  
 L. Grillo<sup>56</sup>, L. Gruber<sup>40</sup>, B.R. Gruberg Cazon<sup>57</sup>, O. Grünberg<sup>67</sup>,  
 E. Gushchin<sup>34</sup>, Yu. Guz<sup>37</sup>, T. Gys<sup>40</sup>, C. Göbel<sup>62</sup>, T. Hadavizadeh<sup>57</sup>,  
 C. Hadjivasiliou<sup>5</sup>, G. Haefeli<sup>41</sup>, C. Haen<sup>40</sup>, S.C. Haines<sup>49</sup>,  
 B. Hamilton<sup>60</sup>, X. Han<sup>12</sup>, T.H. Hancock<sup>57</sup>, S. Hansmann-Menzemer<sup>12</sup>,  
 N. Harnew<sup>57</sup>, S.T. Harnew<sup>48</sup>, C. Hasse<sup>40</sup>, M. Hatch<sup>40</sup>, J. He<sup>63</sup>,  
 M. Hecker<sup>55</sup>, K. Heinicke<sup>10</sup>, A. Heister<sup>9</sup>, K. Hennessy<sup>54</sup>, P. Henrard<sup>5</sup>,  
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 P.H. Hopchev<sup>41</sup>, W. Hu<sup>65</sup>, W. Huang<sup>63</sup>, Z.C. Huard<sup>59</sup>, W. Hulsbergen<sup>43</sup>,  
 T. Humair<sup>55</sup>, M. Hushchyn<sup>35</sup>, D. Hutchcroft<sup>54</sup>, P. Ibis<sup>10</sup>, M. Idzik<sup>28</sup>,  
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 N. Kazeev<sup>35</sup>, M. Kecke<sup>12</sup>, F. Keizer<sup>49</sup>, M. Kelsey<sup>61</sup>, M. Kenzie<sup>49</sup>,  
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 S. Klaver<sup>19</sup>, K. Klimaszewski<sup>29</sup>, T. Klimovich<sup>11</sup>, S. Koliiev<sup>46</sup>,  
 M. Kolpin<sup>12</sup>, R. Kopečna<sup>12</sup>, P. Koppenburg<sup>43</sup>, A. Kosmyntseva<sup>32</sup>,  
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 C. Langenbruch<sup>9</sup>, T. Latham<sup>50</sup>, C. Lazzeroni<sup>47</sup>, R. Le Gac<sup>6</sup>,  
 A. Leflat<sup>33,40</sup>, J. Lefrançois<sup>7</sup>, R. Lefèvre<sup>5</sup>, F. Lemaitre<sup>40</sup>,  
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 F. Machefert<sup>7</sup>, F. Maciuc<sup>30</sup>, V. Macko<sup>41</sup>, P. Mackowiak<sup>10</sup>,  
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 M.W. Majewski<sup>28</sup>, S. Malde<sup>57</sup>, B. Malecki<sup>27</sup>, A. Malinin<sup>68</sup>,  
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 M. Marinangeli<sup>41</sup>, P. Marino<sup>41</sup>, J. Marks<sup>12</sup>, G. Martellotti<sup>26</sup>, M. Martin<sup>6</sup>,  
 M. Martinelli<sup>41</sup>, D. Martinez Santos<sup>39</sup>, F. Martinez Vidal<sup>70</sup>,  
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 A. McNab<sup>56</sup>, R. McNulty<sup>13</sup>, J.V. Mead<sup>54</sup>, B. Meadows<sup>59</sup>, C. Meaux<sup>6</sup>,  
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 E. Michielin<sup>23</sup>, D.A. Milanes<sup>66</sup>, E. Millard<sup>50</sup>, M.-N. Minard<sup>4</sup>,  
 L. Minzoni<sup>17</sup>, D.S. Mitzel<sup>12</sup>, A. Mogini<sup>8</sup>, J. Molina Rodriguez<sup>1</sup>,  
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 M.J. Morello<sup>24,t</sup>, O. Morgunova<sup>68</sup>, J. Moron<sup>28</sup>, A.B. Morris<sup>52</sup>,  
 R. Mountain<sup>61</sup>, F. Muheim<sup>52</sup>, M. Mulder<sup>43</sup>, D. Müller<sup>56</sup>, J. Müller<sup>10</sup>,  
 K. Müller<sup>42</sup>, V. Müller<sup>10</sup>, P. Naik<sup>48</sup>, T. Nakada<sup>41</sup>, R. Nandakumar<sup>51</sup>,  
 A. Nandi<sup>57</sup>, I. Nasteva<sup>2</sup>, M. Needham<sup>52</sup>, N. Neri<sup>22,40</sup>, S. Neubert<sup>12</sup>,  
 N. Neufeld<sup>40</sup>, M. Neuner<sup>12</sup>, T.D. Nguyen<sup>41</sup>, C. Nguyen-Mau<sup>41,n</sup>,  
 S. Nieswand<sup>9</sup>, R. Niet<sup>10</sup>, N. Nikitin<sup>33</sup>, T. Nikodem<sup>12</sup>, A. Nogay<sup>68</sup>,  
 D.P. O’Hanlon<sup>50</sup>, A. Oblakowska-Mucha<sup>28</sup>, V. Obraztsov<sup>37</sup>, S. Ogilvy<sup>19</sup>,  
 R. Oldeman<sup>16,f</sup>, C.J.G. Onderwater<sup>71</sup>, A. Ossowska<sup>27</sup>,  
 J.M. Otalora Goicochea<sup>2</sup>, P. Owen<sup>42</sup>, A. Oyanguren<sup>70</sup>, P.R. Pais<sup>41</sup>,  
 A. Palano<sup>14</sup>, M. Palutan<sup>19,40</sup>, A. Papanestis<sup>51</sup>, M. Pappagallo<sup>52</sup>,  
 L.L. Pappalardo<sup>17,g</sup>, W. Parker<sup>60</sup>, C. Parkes<sup>56</sup>, G. Passaleva<sup>18,40</sup>,  
 A. Pastore<sup>14,d</sup>, M. Patel<sup>55</sup>, C. Patrignani<sup>15,e</sup>, A. Pearce<sup>40</sup>, A. Pellegrino<sup>43</sup>,  
 G. Penso<sup>26</sup>, M. Pepe Altarelli<sup>40</sup>, S. Perazzini<sup>40</sup>, D. Pereima<sup>32</sup>, P. Perret<sup>5</sup>,  
 L. Pescatore<sup>41</sup>, K. Petridis<sup>48</sup>, A. Petrolini<sup>20,h</sup>, A. Petrov<sup>68</sup>,  
 M. Petruzzo<sup>22,q</sup>, E. Picatoste Olloqui<sup>38</sup>, B. Pietrzyk<sup>4</sup>, G. Pietrzyk<sup>41</sup>,  
 M. Pikies<sup>27</sup>, D. Pinci<sup>26</sup>, F. Pisani<sup>40</sup>, A. Pistone<sup>20,h</sup>, A. Piucci<sup>12</sup>,  
 V. Placinta<sup>30</sup>, S. Playfer<sup>52</sup>, M. Plo Casasus<sup>39</sup>, F. Polci<sup>8</sup>, M. Poli Lener<sup>19</sup>,  
 A. Poluektov<sup>50</sup>, I. Polyakov<sup>61</sup>, E. Polycarpo<sup>2</sup>, G.J. Pomery<sup>48</sup>, S. Ponce<sup>40</sup>,  
 A. Popov<sup>37</sup>, D. Popov<sup>11,40</sup>, S. Poslavskii<sup>37</sup>, C. Potterat<sup>2</sup>, E. Price<sup>48</sup>,  
 J. Prisciandaro<sup>39</sup>, C. Prouve<sup>48</sup>, V. Pugatch<sup>46</sup>, A. Puig Navarro<sup>42</sup>,  
 H. Pullen<sup>57</sup>, G. Punzi<sup>24,p</sup>, W. Qian<sup>50</sup>, J. Qin<sup>63</sup>, R. Quagliani<sup>8</sup>,  
 B. Quintana<sup>5</sup>, B. Rachwal<sup>28</sup>, J.H. Rademacker<sup>48</sup>, M. Rama<sup>24</sup>,  
 M. Ramos Pernas<sup>39</sup>, M.S. Rangel<sup>2</sup>, I. Raniuk<sup>45,†</sup>, F. Ratnikov<sup>35</sup>,  
 G. Raven<sup>44</sup>, M. Ravonel Salzgeber<sup>40</sup>, M. Reboud<sup>4</sup>, F. Redi<sup>41</sup>,  
 S. Reichert<sup>10</sup>, A.C. dos Reis<sup>1</sup>, C. Remon Alepuz<sup>70</sup>, V. Renaudin<sup>7</sup>,  
 S. Ricciardi<sup>51</sup>, S. Richards<sup>48</sup>, M. Rihl<sup>40</sup>, K. Rinnert<sup>54</sup>, P. Robbe<sup>7</sup>,  
 A. Robert<sup>8</sup>, A.B. Rodrigues<sup>41</sup>, E. Rodrigues<sup>59</sup>, J.A. Rodriguez Lopez<sup>66</sup>,

A. Rogozhnikov<sup>35</sup>, S. Roiser<sup>40</sup>, A. Rollings<sup>57</sup>, V. Romanovskiy<sup>37</sup>,  
 A. Romero Vidal<sup>39,40</sup>, M. Rotondo<sup>19</sup>, M.S. Rudolph<sup>61</sup>, T. Ruf<sup>40</sup>,  
 P. Ruiz Valls<sup>70</sup>, J. Ruiz Vidal<sup>70</sup>, J.J. Saborido Silva<sup>39</sup>, E. Sadykhov<sup>32</sup>,  
 N. Sagidova<sup>31</sup>, B. Saitta<sup>16,f</sup>, V. Salustino Guimaraes<sup>62</sup>,  
 C. Sanchez Mayordomo<sup>70</sup>, B. Sanmartin Sedes<sup>39</sup>, R. Santacesaria<sup>26</sup>,  
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 S. Schael<sup>9</sup>, M. Schellenberg<sup>10</sup>, M. Schiller<sup>53</sup>, H. Schindler<sup>40</sup>,  
 M. Schmelling<sup>11</sup>, T. Schmelzer<sup>10</sup>, B. Schmidt<sup>40</sup>, O. Schneider<sup>41</sup>,  
 A. Schopper<sup>40</sup>, H.F. Schreiner<sup>59</sup>, M. Schubiger<sup>41</sup>, M.H. Schune<sup>7</sup>,  
 R. Schwemmer<sup>40</sup>, B. Sciascia<sup>19</sup>, A. Sciubba<sup>26,k</sup>, A. Semennikov<sup>32</sup>,  
 E.S. Sepulveda<sup>8</sup>, A. Sergi<sup>47</sup>, N. Serra<sup>42</sup>, J. Serrano<sup>6</sup>, L. Sestini<sup>23</sup>,  
 P. Seyfert<sup>40</sup>, M. Shapkin<sup>37</sup>, I. Shapoval<sup>45</sup>, Y. Shcheglov<sup>31</sup>, T. Shears<sup>54</sup>,  
 L. Shekhtman<sup>36,w</sup>, V. Shevchenko<sup>68</sup>, B.G. Siddi<sup>17</sup>, R. Silva Coutinho<sup>42</sup>,  
 L. Silva de Oliveira<sup>2</sup>, G. Simi<sup>23,o</sup>, S. Simone<sup>14,d</sup>, M. Sirendi<sup>49</sup>,  
 N. Skidmore<sup>48</sup>, T. Skwarnicki<sup>61</sup>, I.T. Smith<sup>52</sup>, J. Smith<sup>49</sup>, M. Smith<sup>55</sup>,  
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 S. Stahl<sup>40</sup>, P. Stefko<sup>41</sup>, S. Stefkova<sup>55</sup>, O. Steinkamp<sup>42</sup>, S. Stemmler<sup>12</sup>,  
 O. Stenyakin<sup>37</sup>, M. Stepanova<sup>31</sup>, H. Stevens<sup>10</sup>, S. Stone<sup>61</sup>, B. Storaci<sup>42</sup>,  
 S. Stracka<sup>24,p</sup>, M.E. Stramaglia<sup>41</sup>, M. Straticiuc<sup>30</sup>, U. Straumann<sup>42</sup>,  
 J. Sun<sup>3</sup>, L. Sun<sup>64</sup>, K. Swientek<sup>28</sup>, V. Syropoulos<sup>44</sup>, T. Szumlak<sup>28</sup>,  
 M. Szymanski<sup>63</sup>, S. T’Jampens<sup>4</sup>, A. Tayduganov<sup>6</sup>, T. Tekampe<sup>10</sup>,  
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 A. Valassi<sup>40</sup>, S. Valat<sup>40</sup>, G. Valenti<sup>15</sup>, R. Vazquez Gomez<sup>40</sup>,  
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